

Ligações Aparafusadas

Terceira Parte



Programa de Pós-Graduação em Engenharia Civil

PGECIV - Mestrado Acadêmico

Faculdade de Engenharia – FEN/UERJ

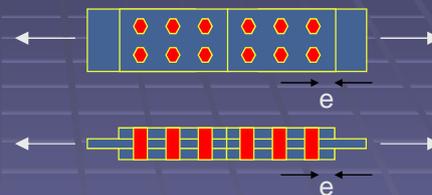
Disciplina: Tópicos Especiais em Projeto (Ligações em Aço e Mistras)

Professor: Luciano Rodrigues Ornelas de Lima

11. Dimensionamento

■ Esmagamento da chapa

$$B_r < \begin{cases} \text{esmagamento} \\ 3 \phi_{br} t n d F_u \\ \text{rasgamento} \\ \phi_{br} t n e F_u \end{cases}$$



$$\phi_{br} = 0,67$$

d = diâmetro do parafuso

n = nº de parafusos

t = espessura de chapara a ser analisada

F_u = tensão última da placa

e = distância do furo a borda na direção paralela ao esmagamento

3

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- Corte no parafuso

$V_r = 0,60 \phi_b n m A_b F_u$ (rosca fora do plano de corte)

$V_r = 0,70 \cdot 0,60 \phi_b n m A_b F_u$ (rosca no plano de corte)

$\phi_b = 0,80$

$m = n^\circ$ de planos de corte

$n = n^\circ$ de parafusos

$A_b = \text{área da seção transversal do parafuso (bruta)}$

$F_u = \text{tensão última do parafuso}$

$V_{\text{final}} < \begin{cases} V_r \\ B_r \end{cases}$

Se o comprimento da ligação > 1300 mm $\rightarrow V_{\text{corr}} = 0,8 V_{\text{final}}$

4

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- Resistência ao Cisalhamento Eurocode 3 pt. 1.8
- a) Category A: Bearing type:
 - ✓ Bolts from class 4.6 up to and including class 10.9 should be used.
 - ✓ No preloading/ special provisions for contact surfaces are required.
 - ✓ The design ultimate shear load \leq shear and/or bearing resistance.

Table 3.2: Categories of bolted connections

Category	Criteria	Remarks
Shear connections		
A bearing type	$F_{v,Ed} \leq F_{v,Rd}$ $F_{v,Ed} \leq F_{b,Rd}$	No preloading required. Bolt classes from 4.6 to 10.9 may be used.

5

11. Dimensionamento

- Resistência ao Cisalhamento Eurocode 3 pt. 1.8
- a) Category A: Bearing type:

A bearing type	$\frac{F_{v,Ed}}{F_{v,Rd}} \leq \frac{F_{v,Rd}}{F_{b,Rd}}$	No preloading required. Bolt classes from 4.6 to 10.9 may be used.
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Table 3.4: Design resistance for individual fasteners subjected to shear and/or tension

Failure mode	Bolts	Rivets
Shear resistance per shear plane	$F_{v,Rd} = \frac{\alpha_v f_{ub} A}{\gamma_{M2}}$ <ul style="list-style-type: none"> - where the shear plane passes through the threaded portion of the bolt (A is the tensile stress area of the bolt A_s): - for classes 4.6, 5.6 and 8.8: $\alpha_v = 0,6$ - for classes 4.8, 5.8, 6.8 and 10.9: $\alpha_v = 0,5$ - where the shear plane passes through the unthreaded portion of the bolt (A is the gross cross section of the bolt): $\alpha_v = 0,6$ 	$F_{v,Rd} = \frac{0,6 f_{ur} A_0}{\gamma_{M2}}$

5

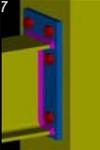
 

11. Dimensionamento

- Resistência ao Cisalhamento Eurocode 3 pt. 1.8
- a) Category A: Bearing type:

A bearing type	$\frac{F_{v,Ed}}{F_{v,Rd}} \leq \frac{F_{v,Rd}}{F_{b,Rd}}$	No preloading required. Bolt classes from 4.6 to 10.9 may be used.
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Bearing resistance ^{1), 2), 3)}	$F_{b,Rd} = \frac{k_1 a_b f_u d t}{\gamma_{M2}}$ <p>where a_b is the smallest of $\alpha_d \frac{f_{ub}}{f_u}$ or 1,0;</p> <p>in the direction of load transfer:</p> <ul style="list-style-type: none"> - for end bolts: $\alpha_d = \frac{e_1}{3d_0}$; for inner bolts: $\alpha_d = \frac{p_1}{3d_0} - \frac{1}{4}$ <p>perpendicular to the direction of load transfer:</p> <ul style="list-style-type: none"> - for edge bolts: k_1 is the smallest of $2,8 \frac{e_2}{d_0} - 1,7$ or 2,5 - for inner bolts: k_1 is the smallest of $1,4 \frac{p_2}{d_0} - 1,7$ or 2,5
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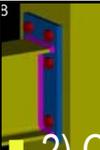


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- 1) Bearing resistance $F_{b,Rd}$ for bolts:
 - ✓ bearing resistance in oversized holes is 0,8 x resistance for normal holes.
 - ✓ in slotted holes, where the longitudinal axis of the slotted hole is perpendicular to the direction of the force transfer, is 0,6 times the bearing resistance for bolts in round, normal holes.



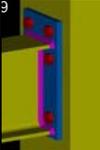
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- 2) Countersunk bolt:
 - ✓ Bearing resistance $F_{b,Rd}$ should be based on a plate thickness = thickness of the connected plate – $\frac{1}{2}$ countersinking depth.
 - ✓ Tension resistance $F_{t,Rd}$ the angle/depth of countersinking should conform with 2.8 Ref. Standards: Group 4, otherwise tension resistance $F_{t,Rd}$ should be adjusted accordingly.
- 3) When the load on a bolt is not \parallel edge:
 - ✓ Bearing resistance may be verified separately for bolt load components \parallel and \perp to the end

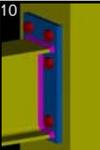
9



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- Design resistances for tension and for shear through the threaded portion of a bolt given in Table 3.4 should only be used for bolts manufactured in conformity with 2.8 Ref. Standard: Group 4.
- For bolts with cut threads, such as anchor bolts or tie rods fabricated from round steel bars where the threads comply with EN1090, the relevant values from Table 3.4 should be used.

10



11. Dimensionamento

- Bolts with cut threads where the threads do not comply with EN1090 relevant values from Table 3.4 should be multiplied by a factor of 0,85.
- Shear resistance $F_{v,Rd}$ given in Table 3.4 should only be used where the bolts are used in holes with nominal clearances not exceeding those for normal holes as specified in 2.8 Ref. Standards: Group 7.

11

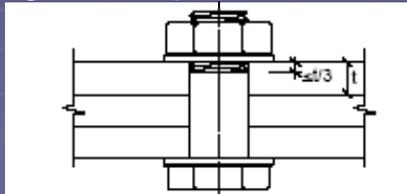
11. Dimensionamento

- M12 and M14 bolts may also be used in 2 mm clearance holes provided that the bolt group resistance based on bearing is \geq bolt group resistance based on bolt shear.
- In addition for class 4.8, 5.8, 6.8, 8.8 and 10.9 bolts the shear resistance F_v, R_d should be taken as 0,85 x value given in Table 3.4

12

11. Dimensionamento

- Fit bolts
 - Should be designed as bolts in normal holes
 - Fit bolt thread should not be included in the shear plane
 - Length of the threaded portion of a fit bolt included in the bearing length $\leq 1/3$ plate thickness



- Hole tolerance \rightarrow 2.8 Ref. Standards: Group 7.

13

11. Dimensionamento

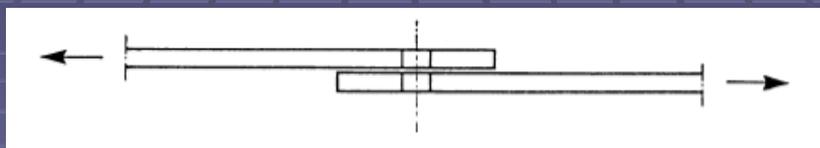
- In single lap joints with only one bolt row the bolts should be provided with washers under both the head and the nut. The bearing resistance $F_{b,Rd}$ for each bolt should be limited to:

$$F_{b,Rd} \leq 1,5 f_u d t / \gamma_{M2} \quad (3.2)$$

14

11. Dimensionamento

- Single rivets should not be used in single lap joints.

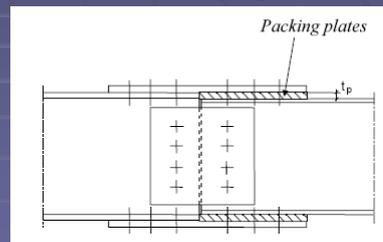


- In the case of class 8.8 or 10.9 bolts, hardened washers should be used for single lap joints with only one bolt or one row of bolts

11. Dimensionamento

- Where bolts or rivets transmitting load in shear and bearing pass through packing of total thickness $p > 1/3$ of the nominal diameter the shear resistance F_v, R_d calculated as specified in Table 3.4, should be multiplying by a reduction factor β_p given by:

$$\beta_p = \frac{9d}{8d + 3t_p} \quad \text{but } \beta_p \leq 1 \quad (3.3)$$



- For double shear connections with packing on both sides of the splice, p should be taken as the thickness of the thicker packing

11. Dimensionamento

- Riveted connections should be designed to transfer shear forces. If tension is present the design tensile force F_t, E_d should not exceed the tension resistance F_t, R_d given in Table 3.4.
- For S235 steel grade the "as driven" value of f_u may be taken as 400 N/mm²
- As a general rule, the grip length of a rivet should not exceed 4,5 for hammer riveting and 6,5 for press riveting.

17

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11. Dimensionamento

- Aços Ingleses

Grade	Espessura t <	Tensão de Escoamento Fy (MPa)
43	16	275
	40	265
	100	245
50	16	355
	63	340
	100	325
55	16	450
	25	430
	40	415

18

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11. Dimensionamento

- Norma Inglesa BS5950 - Edificações

Bolt capacities

Nom. dia. (mm)	Stress area (mm ²)	Tension (kN)	Shear ^a (kN)		Bearing ^b (Grade 43/Grade 50) (kN)					
			Single	Double	6 mm	8 mm	10 mm	12 mm	15 mm	20 mm
4.6 bolts										
12	84.3	16.4	13.5	27	31.3/31.3					
16	157	30.6	25.1	50.2	41.8/41.8	55.7/55.7				
20	245	47.8	39.2	78.4	52.2/52.2	69.6/69.6	87/87			
24	353	68.8	56.5	113.0	62.6/62.6	83.5/83.5	104.4/104.4	125.3/125.3		
30	561	109.4	89.8	179.5	78.3/78.3	104.4/104.4	130.5/130.5	156.6/156.6	195.7/195.7	
8.8 bolts										
12	84.3	37.9	31.6	63.2	33.1/39.6	44.2/52.3	55.2/66	66.2/—		
16	157	70.7	58.9	117.7	44.2/52.8	58.9/70.4	73.6/93	88.3/105.6	110.4/132	147.2/—
20	245	110.3	91.9	183.7	55.2/66	73.6/98	92/110	110.4/132	133/165	184/220
24	353	158.9	132.4	264.7	66.2/79.2	88.3/105.6	110.4/132	132.5/158.4	166/198	220.3/264
30	561	252	210.4	420.7	82.8/99	110.4/132	133/165	166/198	217/247.5	276/330

^aAssumes threads in both shear planes.
^bAssumes end distance not less than 1d.

Table 5.1 Design data for ordinary bolts to BS 5950: Part 1

Design strengths

Bolt grade	4.6		8.8	
	43	50	43	50
Tension p_t	195	195	450	450
Shear p_s	160	160	375	375
Bearing on connected ply p_{bc}	(460)	(550)	460	550
Bearing on bolt p_{bb}	435	435	(970)	(970)

11. Dimensionamento

■ Norma Inglesa BS5400 - Pontes

Table 5.2 Design strengths of bearing bolts according to BS 5400: Part 3 (ultimate limit state)

Bolt grade	4.6	8.8
Tension σ_t	$\frac{235}{1.2 \times 1.1} = 178$	$\frac{549.5}{1.2 \times 1.1} = 416$
Shear σ_s	$\frac{0.85 \times 235}{1.1 \times 1.1 \times \sqrt{2}} = 116.7$	$\frac{0.85 \times 549.5}{1.1 \times 1.1 \times \sqrt{2}} = 273$
Bearing ^b $k_1 k_2 k_3 k_4 \sigma_b$	$\frac{0.85 \times 1.97 \times 1.2 \times 1.0 \times 235}{1.05 \times 1.1} = 499 \text{ N/mm}^2$	$\frac{0.85 \times 1.97 \times 1.2 \times 1.0 \times 275}{1.05 \times 1.1} = 478 \text{ N/mm}^2$
<small>(Grade 43, L = 2d, T < 16 mm)</small>		

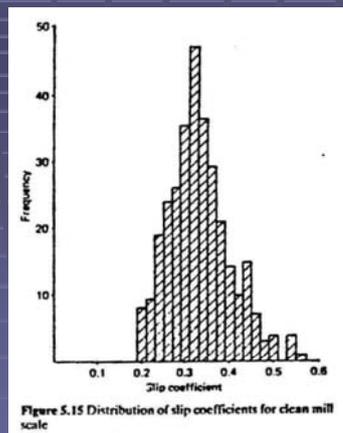
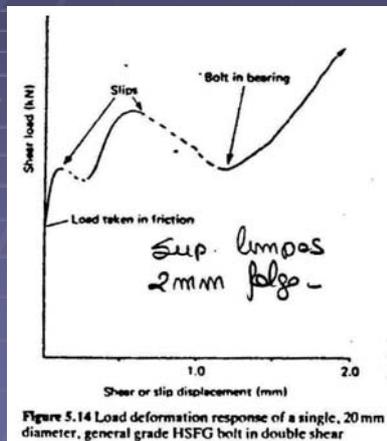
Bolt capacities

Nom. dia. (mm)	Stress area (mm ²)	Tension		Shear ^a		b mm	Bearing ^b (Grade 43/Grade 50 for 8.8 bolts)				
		(kN)	(kN)	Single (kN)	Double (kN)		8 mm	10 mm	12 mm	15 mm	20 mm
4.6 bolts											
12	84.3	15.0	9.8	19.7	29.4						
16	157	27.9	18.3	36.6	39.2						
20	245	44.6	28.6	57.2	49.0	65.3					
24	353	62.8	41.2	82.4	58.8	76.3	97.9				
30	561	99.9	65.5	131.9	73.4	98.0	122	147			
8.8 bolts											
12	84.3	35.1	23	46.0	34.4/44.4	45.9/—					
16	157	65.3	42.8	85.3	45.9/59.2	61.1/79.0	76.4/98.8	91.8/—			
20	245	102	66.9	133	57.4/74.0	76.4/98.8	95.2/123	114/148	143/—		
24	353	147	96	193	68.8/98.8	91.7/118	114/148	136/178	172/222	221/—	
30	561	233	153	306	86.0/111	115/148	143/185	172/222	214/277	277/360	346/—

^aAssumes threads in both shear planes.
^bEach bolt bearing value with an end distance of 2 x d

11. Dimensionamento

■ Atrito



Coeficiente de atrito médio = 0.45?

11. Dimensionamento

- Valores típicos para os coeficientes de atrito → superfícies de contacto

Table 5.3 Typical average values for coefficients of friction

Clean mill scale	0.33
Grades 43 or 50, grit or shot blasted	0.48
Ditto, after light rusting	0.52
Very high tensile steel, grit blasted	0.33
Red lead paint	0.1 or less
Grit blasted and oiled	0.25
Galvanized	0.22
Galvanized, subsequently wire brushed or grit blasted	0.41
Metal sprayed with zinc	0.46
Metal sprayed with aluminium	0.51
Metal sprayed aluminium on zinc	0.49
Surfaces painted with alkali-zinc silicate coat (50-80 mm)	0.46



Óleos (furação) →
 Lubrificantes (tintas) →
 rugosidade da superfície →
 Pouca ferrugem → melhora → Interlock
 Muita ferrugem → piora → escamação
 Solda fria

11. Dimensionamento

- Transferência de Pré-tensão por furação desencontrada
- Aperto normal → rotação da porca
- Assume-se $P_{pret} = 70\% P_u$
- Porém $\exists 20$ a 30% de variação
- 3 testes para 2 metades de junta p/ cada um
 - ✓ Menor valor
 - ✓ Valor característico

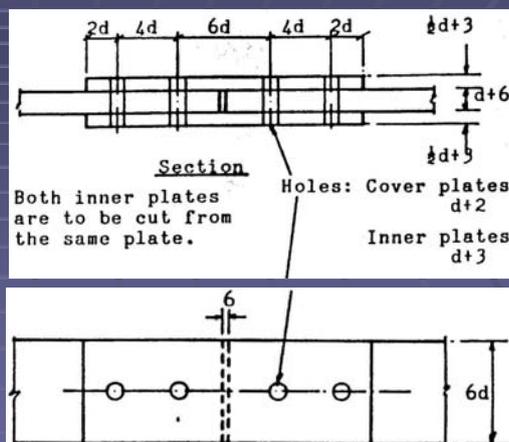
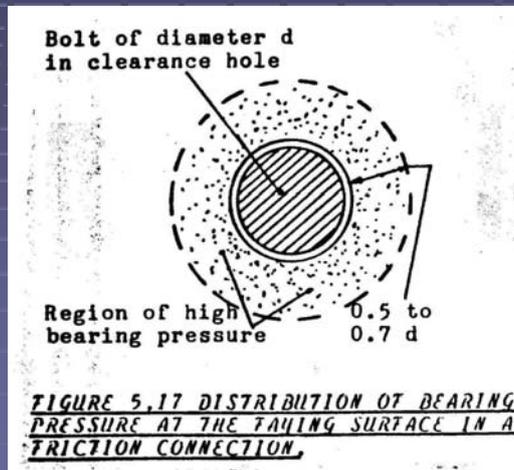


FIGURE 5.16 TEST SPECIMEN DETAILS FOR SLIP COEFFICIENT TESTS.

11. Dimensionamento

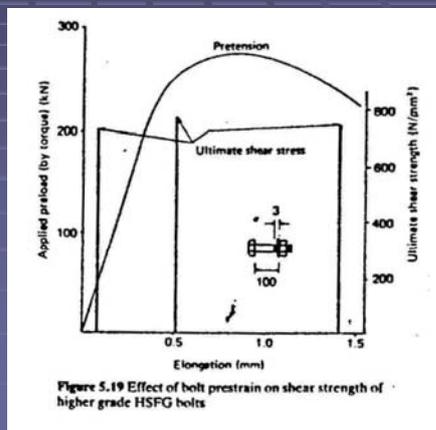
- Atrito → pressão de contacto → arruela
- Anel (rugosidade) → escoar sob compressão → superfícies polidas
- atrito ↔ pressão de contacto
- $\mu \downarrow$ com furos alargados → área de contacto menor



11. Dimensionamento

- Influência da carga de pré-tensão na resistência ao cisalhamento pós-atrito

- Interação pré-tensão \times τ_{ult}
- \neq níveis de pré-tensão mesma τ_{ult} sem rosca no plano de corte
- \neq pontos de ruína
- Com rosca no plano de corte → limitada
- Antes da estricção \nexists efeito → cisalhamento → $P_{pret} \downarrow$



11. Dimensionamento

- Relaxação da protensão → carga de atrito
- espessura placas de junta
- s de tração nas placas
- Caso 1 → extremidade (interna + solicitada)
- Caso 2 → centro (externa + solicitada)
- Inicialmente a relaxação é pequena devido a redução elástica da espessura devido ao efeito de Poisson
- $\sigma \uparrow$ relaxação \uparrow

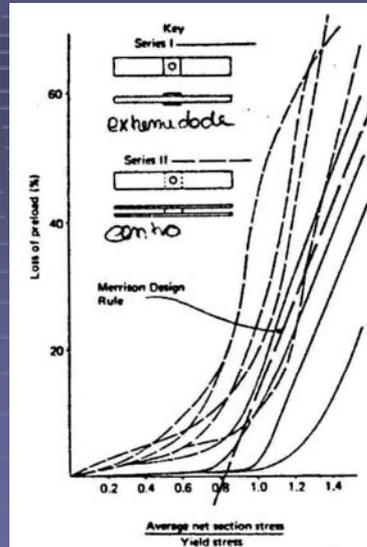


Figure 5.28 Relaxation of bolt preload due to connected plate stresses

11. Dimensionamento

- Transição → $\sigma < F_y$ → concentração da tensão de compressão → P_u (70%)
- Redução pode chegar até valores de 40% → última fila de parafusos (máximo de norma)
- No centro → 10%
- Merrison design rule → σ_n / F_y → relaxação do parafuso
- Com atrito o desalinhamento não é mais problema para distribuição de cisalhamento entre parafusos

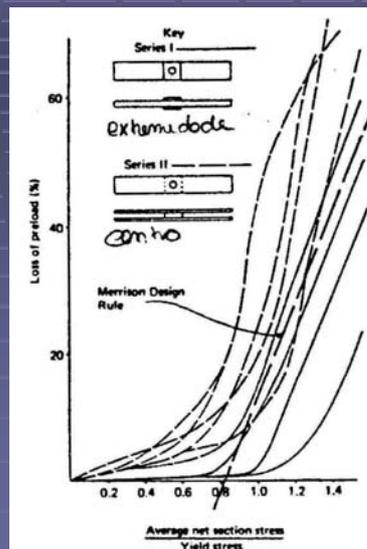


Figure 5.28 Relaxation of bolt preload due to connected plate stresses

11. Dimensionamento

■ Atrito

$$V_s = 0,53 c_1 k_s m n A_b F_u$$

Classe	Descrição	k_s	c_1 (A325)	c_1 (A490)
A	Sem resíduos, limpo com jato de ar com cobertura - classe "A"	0,33	0,82	0,78
B	limpo com jato de ar com cobertura - classe "B"	0,50	0,90	0,85
C	Galvanização por imersão a quente com superfície escovada	0,40	0,90	0,85

k_s = coeficiente de atrito médio (tabelado)

c_1 = coeficiente que relaciona a carga de protensão e o coeficiente de atrito médio k_s a uma probabilidade de escorregamento de 5% para parafusos apertados pelo método da rotação da porca

A e B → $m \geq 0,33$ e $0,5$

11. Dimensionamento

- Atrito – Eurocode 3 pt. 1.8
- b) Category B: Slip-resistant at serviceability limit state
 - ✓ In this category preloaded bolts should be used.
 - ✓ Slip should not occur at the serviceability limit state.
 - ✓ Design serviceability shear load \leq slip resistance
 - ✓ Design ultimate shear load \leq shear resistance
 - ✓ Design ultimate shear load \leq bearing resistance

11. Dimensionamento

- Atrito – Eurocode 3 pt. 1.8
- c) Category C: Slip-resistant at ultimate limit state
 - ✓ In this category preloaded bolts should be used
 - ✓ Slip should not occur at the ultimate limit state
 - ✓ Design ultimate shear load \leq slip resistance
 - ✓ Design ultimate shear load \leq bearing resistance
 - ✓ In addition for a connection in tension, the design plastic resistance of the net cross-section at bolt holes $N_{net,Rd}$, should be checked, at the ultimate limit state.

11. Dimensionamento

- Atrito – Eurocode 3 pt. 1.8

Table 3.2: Categories of bolted connections

Category	Criteria	Remarks
Shear connections		
B slip-resistant at serviceability	$F_{v,Ed,ser} \leq F_{t,Rd,ser}$ $F_{v,Ed} \leq F_{v,Rd}$ $F_{v,Ed} \leq F_{b,Rd}$	Preloaded 8.8 or 10.9 bolts should be used. For slip resistance at serviceability see 3.9.
C slip-resistant at ultimate	$F_{v,Ed} \leq F_{t,Rd}$ $F_{v,Ed} \leq F_{b,Rd}$ $F_{v,Ed} \leq N_{net,Rd}$	Preloaded 8.8 or 10.9 bolts should be used. For slip resistance at ultimate see 3.9. $N_{net,Rd}$ see EN 1993-1-1

11. Dimensionamento

- Resistência ao Atrito Eurocode 3 pt. 1.8
- Categories B and C:

Table 3.4: Design resistance for individual fasteners subjected to shear and/or tension

Failure mode	Bolts	Rivets
Shear resistance per shear plane	$F_{v,Rd} = \frac{\alpha_v \cdot f_{ub} \cdot A}{\gamma_{M2}}$ <ul style="list-style-type: none"> - where the shear plane passes through the threaded portion of the bolt (A is the tensile stress area of the bolt A_s): <ul style="list-style-type: none"> - for classes 4.6, 5.6 and 8.8: $\alpha_v = 0,6$ - for classes 4.8, 5.8, 6.8 and 10.9: $\alpha_v = 0,5$ - where the shear plane passes through the unthreaded portion of the bolt (A is the gross cross section of the bolt): $\alpha_v = 0,6$ 	$F_{v,Rd} = \frac{0,6 \cdot f_{ur} \cdot A_0}{\gamma_{M2}}$

11. Dimensionamento

- Resistência ao Atrito Eurocode 3 pt. 1.8
- Categories B and C:

Bearing resistance ^{1), 2), 3)}	$F_{b,Rd} = \frac{k_1 \cdot a_b \cdot f_u \cdot d \cdot t}{\gamma_{M2}}$ <p>where α_b is the smallest of α_d; $\frac{f_{ub}}{f_u}$ or 1,0;</p> <p>in the direction of load transfer:</p> <ul style="list-style-type: none"> - for end bolts: $\alpha_d = \frac{e_1}{3d_0}$; for inner bolts: $\alpha_d = \frac{p_1}{3d_0} - \frac{1}{4}$ <p>perpendicular to the direction of load transfer:</p> <ul style="list-style-type: none"> - for edge bolts: k_1 is the smallest of $2,8 \frac{e_2}{d_0} - 1,7$ or 2,5 - for inner bolts: k_1 is the smallest of $1,4 \frac{p_2}{d_0} - 1,7$ or 2,5
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11. Dimensionamento

- Atrito – Eurocode 3 pt. 1.8
- Slip-resistant connections using 8.8 or 10.9 bolts
- Design slip resistance of 8.8 or 10.9 bolts should be:

$$F_{s,Rd} = \frac{k_s n \mu}{\gamma_{M3}} F_{p,C} \quad (3.6)$$

- where:
- k_s is given in Table 3.6
- n is the number of the friction surfaces
- m is the slip factor obtained either by specific tests for the friction surface in accordance with 2.8 Reference Standards: Group 7 or given in Table 3.7.

11. Dimensionamento

- Atrito – Eurocode 3 pt. 1.8
- For class 8.8 and 10.9 bolts conforming with 2.8 Reference Standards: Group 4, with controlled tightening in conformity with 2.8 Ref. Standards: Group 7, the preloading force $F_{p,C}$ should be taken as:

$$F_{p,C} = 0,7 f_{ub} A_s \quad (3.7)$$

11. Dimensionamento

■ Atrito – Eurocode 3 pt. 1.8

Table 3.6: Values of k_s

Description	k_s
Bolts in normal holes.	1,0
Bolts in either oversized holes or short slotted holes with the axis of the slot perpendicular to the direction of load transfer.	0,85
Bolts in long slotted holes with the axis of the slot perpendicular to the direction of load transfer.	0,7
Bolts in short slotted holes with the axis of the slot parallel to the direction of load transfer.	0,76
Bolts in long slotted holes with the axis of the slot parallel to the direction of load transfer.	0,63

11. Dimensionamento

■ Atrito – Eurocode 3 pt. 1.8

Table 3.7: Slip factor, μ , for pre-loaded bolts

Class of friction surfaces (see 2.8 Reference Standard: Group 7)	Slip factor μ
A	0,5
B	0,4
C	0,3
D	0,2

NOTE 1: The requirements for testing and inspection are given in 2.8 Reference Standards: Group 7.

NOTE 2: The classification of any other surface treatment should be based on test specimens representative of the surfaces used in the structure using the procedure set out in 2.8 Reference Standards: Group 7.

NOTE 3: The definitions of the class of friction surface are given in 2.8 Reference Standards: Group 7.

NOTE 4: With painted surface treatments account should be made for any loss of pre-load which occur over time.

11. Dimensionamento

■ Atrito - Norma Inglesa BS5950 - Edificações

Table 5.4 Design data for general grade HSFG bolts to BS 5950: Part 1
Basic equations (using notation of BS 5950: Part 1)

$$\begin{aligned} \text{Tension } P_t &= 0.9 P_u \\ \text{Slip } P_{sl} &= 1.1 K_{sl} P_u \\ \text{Combined shear and tension } & \frac{F_u}{P_{sl}} + 0.8 \frac{F_t}{P_t} \leq 1.0 \end{aligned}$$

Design capacities							
Nominal dia. (mm)	16	20	22	24	27	30	36
Proof load (kN)	92.1	144	177	207	234	296	418
Tension capacity (kN)	82.9	129.6	159.3	186.3	210.6	257.4	376.2
Slip capacity (kN)	45.6	71.3	87.6	102.5	115.8	141.6	206.9
External tension (kN)							
25	34.6	60.3	76.6	91.5	104.8	130.6	195.9
50	23.6	49.3	65.6	80.5	93.8	119.6	184.9
75	12.6	38.3	54.6	69.5	82.8	108.6	173.9
100	9.10						
125		27.3	43.6	58.5	71.8	97.6	162.9
129.6		16.3	32.6	47.5	60.8	86.6	151.9
150		14.30					
175			21.6	36.5	49.8	75.6	140.9
186.3			17.50				
200				25.5	33.8	64.6	129.9
210.6				20.50			
Change in interpolation interval							
250						31.6	96.9
257.4						26.50	
300							74.9
350							52.9
376.2							41.60

Assumes a coefficient of friction of 0.45.

11. Dimensionamento

■ Atrito - Norma Inglesa BS5400 - Pontes

Table 5.5 Design data for general grade HSFG bolts to BS 5400: Part 3
Basic equations (using notation of BS 5400: Part 3)

$$\begin{aligned} \text{Tension } P_t &= \frac{0.7 \times 827}{1.2 \times 1.1} A_{st} && \leq M24 \\ &= \frac{0.7 \times 725}{1.2 \times 1.1} A_{st} && > M24 \\ \text{Slip } P_{sl} &= \frac{587.0 \times 0.45}{1.3 \times 1.1} A_{st} && \leq M24 \\ &= \frac{512 \times 0.45}{1.3 \times 1.1} A_{st} && > M24 \\ \text{Combined shear and tension } & F_{st} = \frac{(F_u - F_t) P_{sl}}{T_u T_{st}} \end{aligned}$$

Design capacities							
Nominal diameter (mm)	16	20	22	24	27	30	36
Proof load (kN)	92.1	144	177	207	234	296	418
Tension capacity (kN)	68.9	107.4	132.9	154.8	176.5	215.7	314.1
Slip capacity (kN)	29.0	45.3	56.0	65.2	74.0	90.4	131.6
External tension (kN)							
25	21.1	37.4	48.1	57.3	66.1	82.5	123.7
50	13.3	29.6	40.2	49.5	58.2	74.6	115.9
68.9	7.30						
75		21.7	32.3	41.6	50.3	66.7	108.0
100		13.8	24.4	33.7	42.4	58.8	100.1
107.4		11.50					
125			16.5	25.8	34.5	50.9	92.2
132.9			14.00				
150				18.0	26.6	43.0	84.4
154.8				16.00			
175					18.7	35.1	76.5
176.5					18.20		
200						27.2	68.6
Change in interpolation interval							
215.7							52.9
250							37.2
300							32.70
314.1							

Assumes a coefficient of friction of 0.45.

11. Dimensionamento

- Redução na resistência ao atrito para juntas com furos alongados

Table 5.6 Reduction factors for slip resistance of HSFG bolted joints with non-standard clearance holes

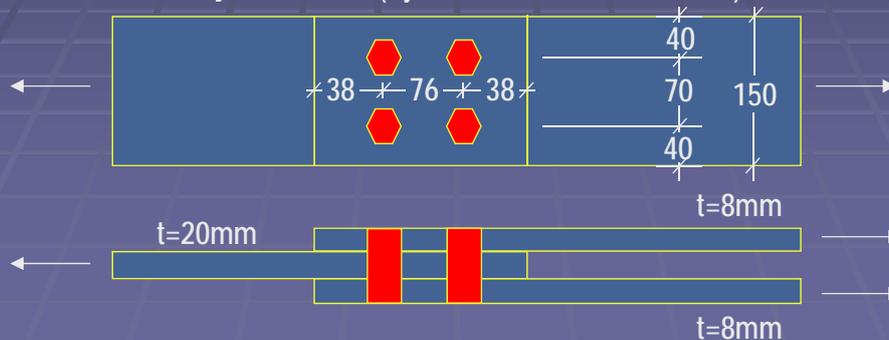
	<i>BS 5950: Part 1</i>	<i>BS 5400: Part 3</i>
Over-size hole	0.85	0.85
Short-slotted hole	0.85	0.85
Long-slotted hole loaded perp. to slot	0.85	0.70
Long-slotted hole loaded parallel to slot	0.60	0.70

12. Exemplos

- Determinar a carga axial máxima de projeto P_d suportada pela ligação aparafusada abaixo. Assumir furos padrão, borda cortada a maçarico e rosca fora do plano de corte.

Dados: $d = 7/8"$ com $F_u = 825\text{MPa}$

Aço ASTM 572 ($F_y = 350\text{MPa}$ e $F_u = 460\text{MPa}$)



12. Exemplos

a) Resistência dos parafusos ao corte

$$d = 7/8" \cdot 25,4\text{mm} = 22,2\text{mm}$$

$$A_b = \pi d^2 / 4 = \pi(22,2)^2 / 4 = 387\text{mm}^2$$

$$V_r = 0,60 \phi_b n m A_b F_u = 0,60 \cdot 0,80 \cdot 1 \cdot 2 \cdot 387 \cdot 0,825 = 306,5\text{kN}$$

$$4 \cdot V_r = 4 \cdot 306,5 = 1226\text{kN}$$

b) Verificação do esmagamento da chapa

menor das espessuras

$$B_r \left\{ \begin{array}{l} 3 \phi_{br} t n d F_u = 3 \cdot 0,67 \cdot (8+8) \cdot 4 \cdot 22,2 \cdot 0,460 = 1313,7\text{kN} \\ \text{esmagamento} \\ \phi_{br} t n e F_u = 0,67 \cdot (8+8) \cdot 4 \cdot 38 \cdot 0,460 = 749,5\text{kN} \\ \text{rasgamento} \end{array} \right.$$

12. Exemplos

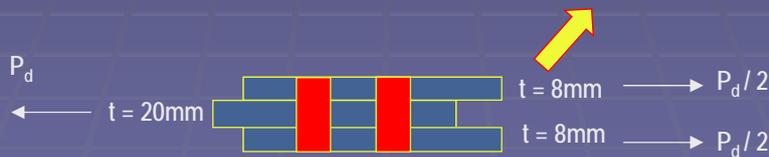
c) Verificação dos espaçamentos

- Furo à borda
 - ✓ $d = 7/8 \cdot 25,4\text{mm} = 22,2\text{mm} \approx 24\text{mm} \rightarrow e > 30\text{mm}$ (borda cortada a maçarico \rightarrow OK)
- Entre furos
 - ✓ $L > 2,7 d = 59,94\text{mm} < 76\text{mm} \rightarrow$ OK
 - ✓ $L > 3 d = 66,6\text{mm}$
 - ✓ $L < 12 t = 12 \cdot 16 = 192\text{mm} > 76\text{mm} \rightarrow$ OK
 - ✓ $L < 150\text{mm}$

12. Exemplos

d) Verificação da placa à tração

- Área bruta
 - ✓ $A_g = 150 \cdot 16 = 2400 \text{mm}^2$
- Área líquida (reduz-se 2 furos com diâmetro 24mm)
 - ✓ $A_g = (150 - 2 \cdot 24) \cdot 16 = 1632 \text{mm}^2$
- Resistência
 - ✓ $T_r = \phi \cdot A_g \cdot F_y = 0,90 \cdot 2400 \cdot 0,350 = 756 \text{kN}$ (escoamento da seção bruta)
 - ✓ $T_r = 0,85 \cdot \phi \cdot A_n \cdot F_u = 0,90 \cdot 1632 \cdot 0,460 = 574,3 \text{kN}$ (ruptura da seção líquida)



12. Exemplos

2. Repetir o exemplo anterior considerando:

- a) Rosca no plano de corte
- b) Ligação por atrito (superfícies limpas → classe "A")

a) Resistência dos parafusos ao corte

$$d = 7/8" \cdot 25,4 \text{mm} = 22,2 \text{mm}$$

$$A_b = \pi d^2 / 4 = \pi (22,2)^2 / 4 = 387 \text{mm}^2$$

$$V_r = 0,70 \cdot 0,60 \cdot \phi_b \cdot n \cdot m \cdot A_b \cdot F_u =$$

$$= 0,70 \cdot 0,60 \cdot 0,80 \cdot 1 \cdot 2 \cdot 387 \cdot 0,825 = 214,5 \text{kN}$$

$$4 \cdot V_r = 4 \cdot 214,5 = 858,2 \text{kN} > T_r \text{ (logo } T_r \text{ ainda controla o dimensionamento)}$$

12. Exemplos

b) Ligação por atrito (superfícies limpas → classe "A")

$$V_s = 0,53 \cdot c_1 \cdot k_s \cdot m \cdot n \cdot A_b \cdot F_u$$

onde $c_1 = 0,82$ e $k_s = 0,33$

$$V_s = 0,53 \cdot 0,82 \cdot 0,33 \cdot 2 \cdot 4 \cdot 387 \cdot 0,825 = 366,32 \text{ kN (não ponderada)} \\ \rightarrow P_d < 366\text{kN})$$